Security and Cryptography just by images

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2009

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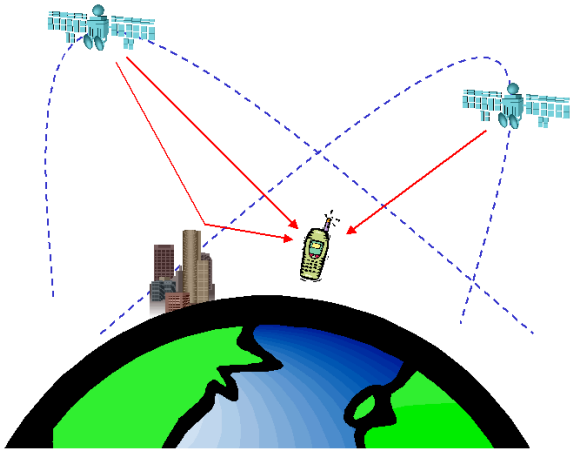
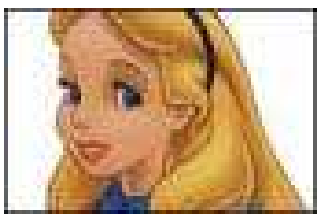
Applications



Secrecy or Confidentiality

Alice communicates with the White rabbit via a network.



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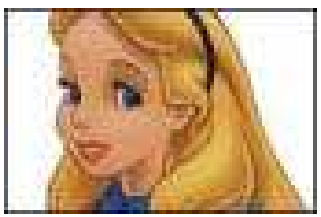
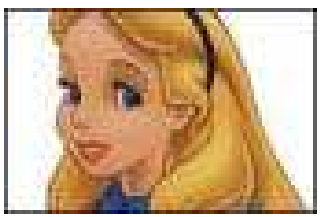


Intruder

Secrecy or Confidentiality

Alice communicates with the White rabbit via a network.

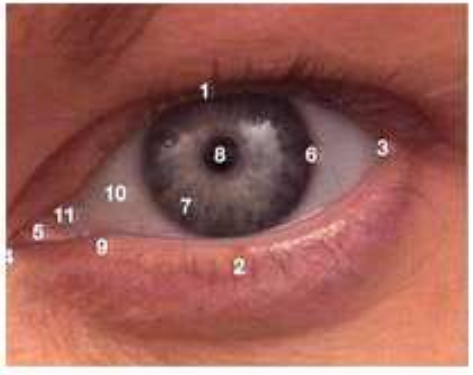


Intruder

Authentication

"On the Internet, nobody knows you're a dog."

Mechanisms for Authentication



1. Something that you know
   E.g. a PIN or a password
2. Something that you have
   E.g. a smart-card
3. Something that you are
   Biometric characteristics like voice, fingerprints, eyes, ...
4. Where you are located
   E.g. in a secure building

Strong authentication combines multiple factors:
E.g., Smart-Card + PIN

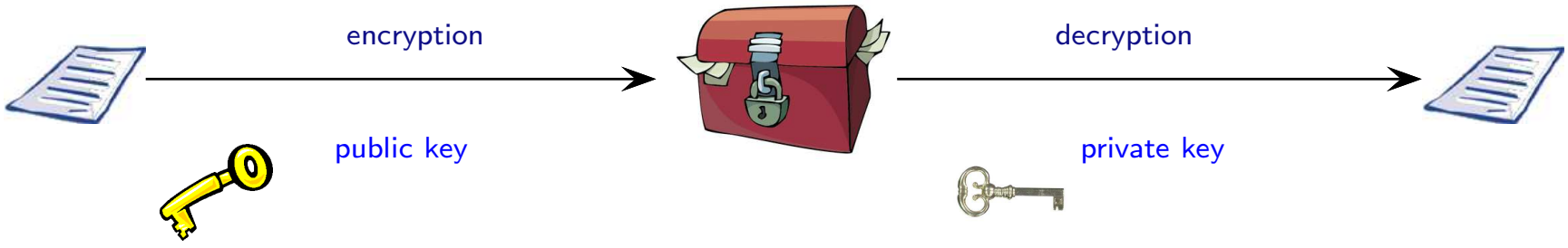
Other security properties

- Integrity: No improper modification of information
- Availability: No improper impairment of functionality/service
- Non-repudiation (also called accountability) is where one can establish responsibility for actions.
- Privacy or Anonymity: secrecy of principal identities or communication relationships.
- etc ...

Symmetric key and public key encryption

- Symmetric key encryption

- Public key encryption



Outline

Motivations

Two Examples

History of Cryptography

Cryptographic Security Intuitions

Logical Attacks

Interactive Zero Knowledge Proofs

Secret Sharing

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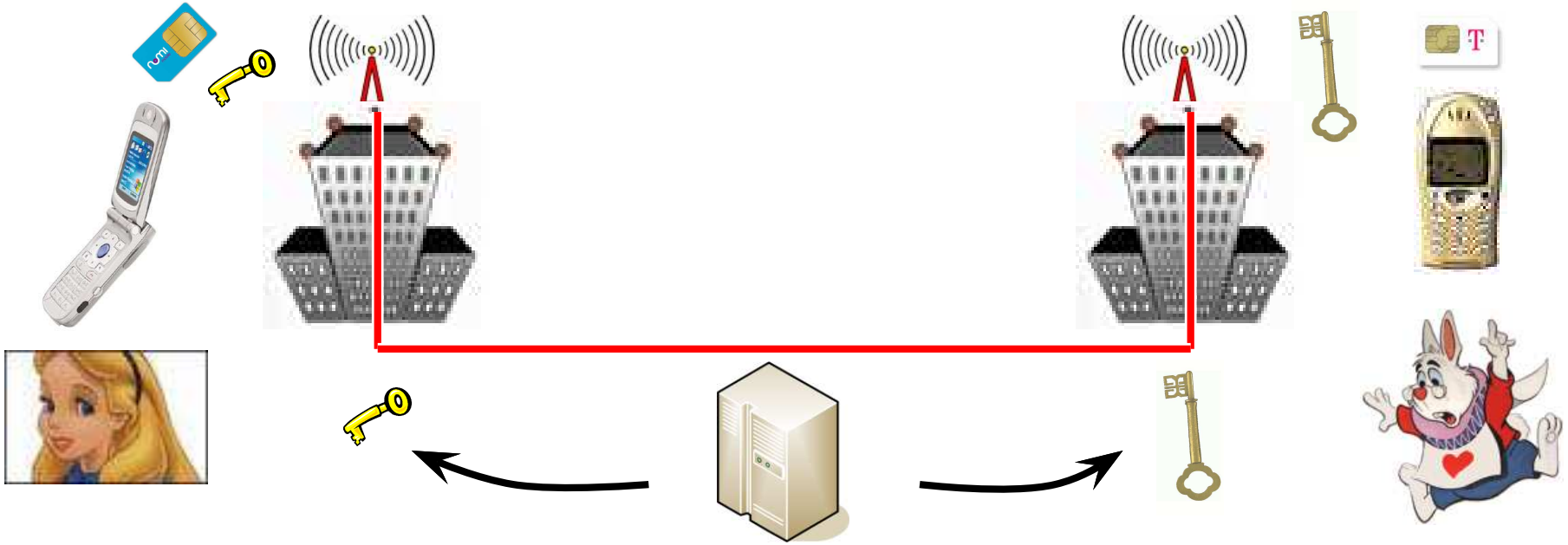
Symetric Encryption for GSM communication



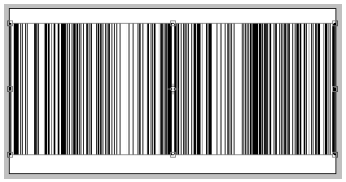
SIM card contains a shared secret key used for authenticating phones and operators, then creating key session for communication.

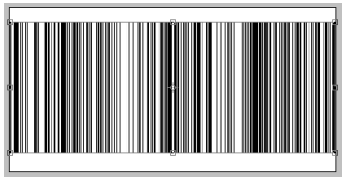
1. Message is encrypted and sent by Alice.
2. The antenna receives the message then uncrypted.
3. Message is encrypted by the antenna with the second key.
4. Second mobile uncrypted the communication.

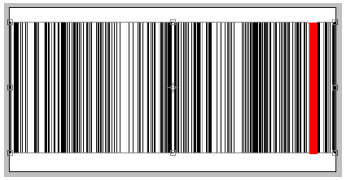
Hash Functions

A hash function H takes as input a bit-string of any finite length and returns a corresponding 'digest' of fixed length.

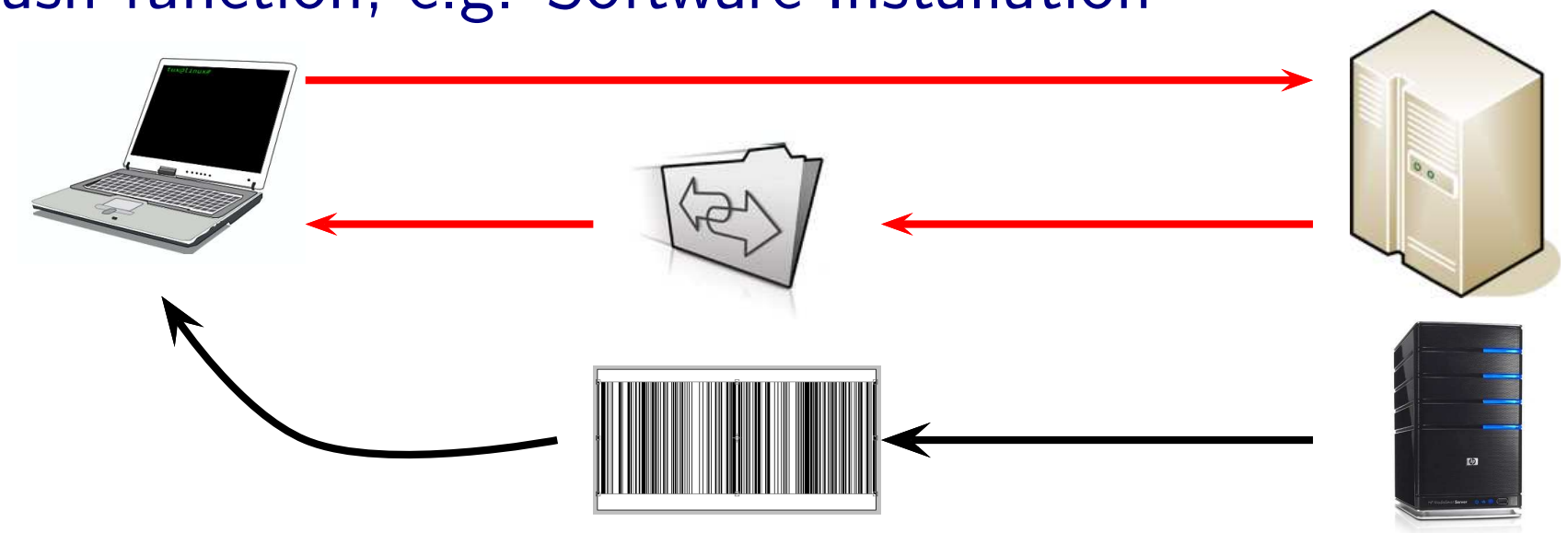
$$H : \{0,1\}^* \rightarrow \{0,1\}^n$$

$H(Alice)$ =  $\neq$ $H(Bob)$

$marion \rightarrow$ 

$marine \nrightarrow$  $\leftarrow$ $laurence$

Hash function, e.g. Software Installation



Integrity of the downloaded file.

1. Download on server 1 the software.
2. Download on server 2 the hash of the software.
3. Check the integrity of the software.

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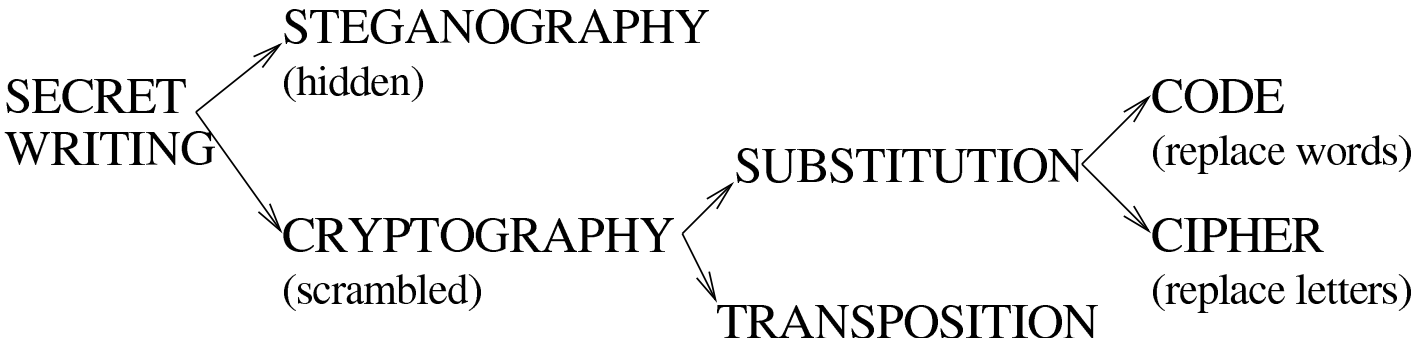
Information hiding



- Cryptology: the study of secret writing.
- Steganography: the science of hiding messages in other messages.
- Cryptography: the science of secret writing.
  Note: terms like encrypt, encode, and encipher are often (loosely and wrongly) used interchangeably

Slave

Historical ciphers

- Used 4000 years ago by Egyptians to encipher hieroglyphics.

- 2000 years ago Julius Caesar used a simple substitution cipher.
- Leon Alberti devised a cipher wheel, and described the principles of frequency analysis in the 1460s.

Substitution cipher examples

- L oryh brx

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- Zngurzngvdhrf = Mathematiques
  ROT13: shift each letter by 13 places.
  Under Unix: tr a-zA-Z n-za-mN-ZA-M.
- 2-25-5 2-25-5

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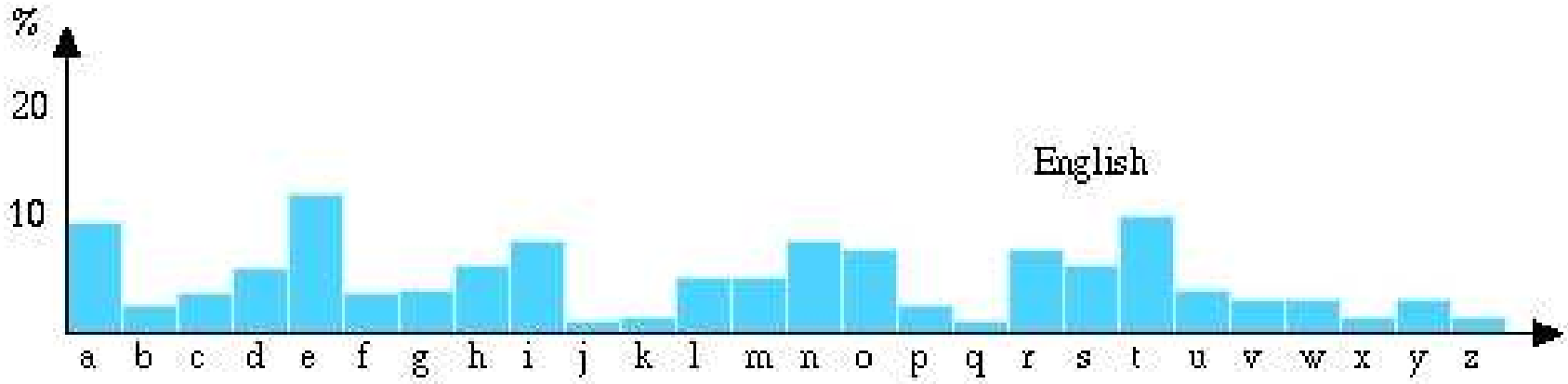
  Under Unix: tr a-zA-Z n-za-mN-ZA-M.
- 2-25-5 2-25-5 = BYE BYE
  Alphanumeric: substitute numbers for letters.

How hard are these to cryptanalyze? Caesar? General?

(In)security of substitution ciphers

- Key spaces are typically huge. 26 letters $\rightsquigarrow$ 26! possible keys.
- Trivial to crack using frequency analysis (letters, digraphs...)
- Frequencies for English based on data-mining books/articles.



Improvement: Homophonic substitution ciphers

$$\mathcal{A} = \{a, b\}$$

$H(a) = \{00, 10\}$, and $H(b) = \{01, 11\}$.

Example

The plaintext ab encrypts to one of 0001, 0011, 1001, 1011.

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Example

The plaintext ab encrypts to one of 0001, 0011, 1001, 1011.

- Rational: makes frequency analysis more difficult.
- Cost: data expansion and more work for decryption.

Polyalphabetic substitution (Leon Alberti, Vignere)

Example: English ($n = 26$), with k = 3,7,10

m = THI SCI PHE RIS CER TAI NLY NOT SEC URE

then

$E_e(m)$ = WOS VJS SOO UPC FLB WHS QSI QVD VLM XYO

Example: transposition ciphers

- $C =$ Aduaenttlydhatoiekounletmtoihahvsekeeeleeyqonouv

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- $C =$ Aduaenttlydhatoiekounletmtoihahvsekeeeleeyqonouv

A	n	d	i	n	t	h	e	e	n
d	t	h	e	l	o	v	e	y	o
u	t	a	k	e	i	s	e	q	u
a	l	t	o	t	h	e	l	o	v
e	y	o	u	m	a	k	e		

Table defines a permutation on 1, ..., 50.

Example: transposition ciphers

- C = Aduaenttlydhatoiekounletmtoihahvsekeeeleeyqonouv

A	n	d	i	n	t	h	e	e	n
d	t	h	e	l	o	v	e	y	o
u	t	a	k	e	i	s	e	q	u
a	l	t	o	t	h	e	l	o	v
e	y	o	u	m	a	k	e		

  Table defines a permutation on 1, ..., 50.
- Idea goes back to Greek Scytale: wrap belt spirally around baton and write plaintext lengthwise on it.

Composite ciphers

- Ciphers based on just substitutions or transpositions are not secure
- Ciphers can be combined. However ...
  - two substitutions are really only one more complex substitution,
  - two transpositions are really only one transposition,
  - but a substitution followed by a transposition makes a new harder cipher.
- Product ciphers chain substitution-transposition combinations.
- Difficult to do by hand
  $\rightsquigarrow$ invention of cipher machines.

One-time pad (Vernam cipher)

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- Example:

$$\begin{array}{rcl} m & = & 010111 \\ k & = & 110010 \\ \hline c & = & 100101 \end{array}$$

- Unconditional (information theoretic) security, if key isn't reused!
- Problem?

One-time pad (Vernam cipher)

- Example:

$$\begin{array}{rcl} m & = & 010111 \\ k & = & 110010 \\ \hline c & = & 100101 \end{array}$$

- Unconditional (information theoretic) security, if key isn't reused!
- Problem? Securely exchanging and synchronizing long keys.

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ECB vs Others

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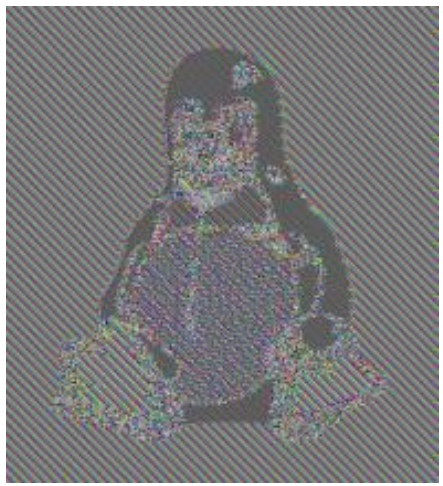
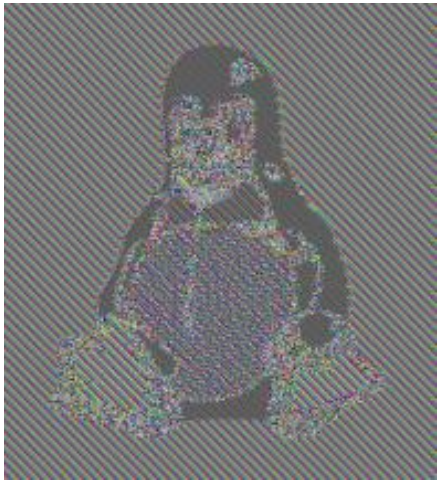
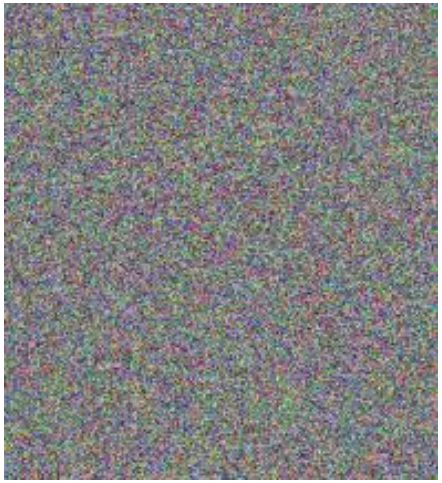


ECB vs Others

One-Wayness (OW)

Put your message in a translucid bag, but you cannot read the text.

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Put your message in a translucid bag, but you cannot read the text.

Without the private key, it is computationally **impossible to recover the plain-text**.

Is it secure ?

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Is it secure ?

- you cannot read the text but you can distinguish which one has been encrypted.

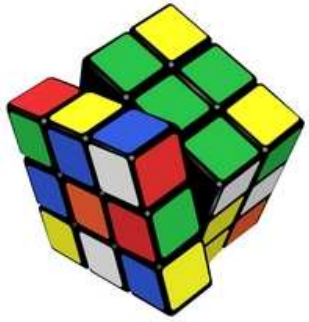
Indistinguishability (IND)

Put your message in a black bag, you can not read anything.

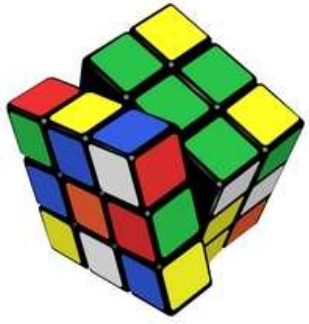
Now a black bag is of course IND and it implies OW.

Is it secure?

Is it secure?



Is it secure?



- It is possible to scramble it in order to produce a new cipher. In more you know the relation between the two plain text because you know the moves you have done.

Non Malleability (NM)

Put your message in a black box.

But in a black box you cannot touch the cube (message), hence NM implies IND.

Summary of Security Notions

Non Malleability

$\Downarrow$

Indistinguishability

$\Downarrow$

One-Wayness

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Attacks

Computational Model
Cryptanalysis

Attacks

Computational Model
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Attacks

Computational Model
Cryptanalysis



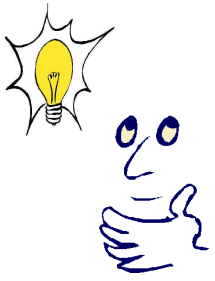


Symbolic Model
Logical Attack

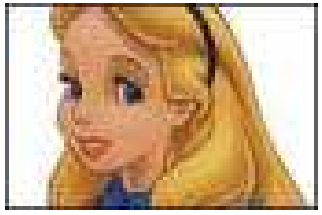
Perfect Encryption hypothesis

Needham-Schroeder Public Key Protocol (1978)

"Man in the middle attack" [Lowe'96]

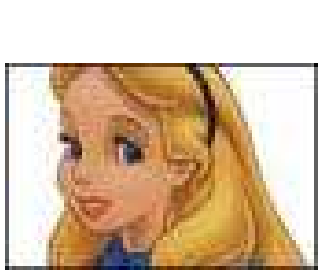


Simple Example



$\{12h10\}_{K_B}$

Simple Example



$\{12h10\}_{K_B}$

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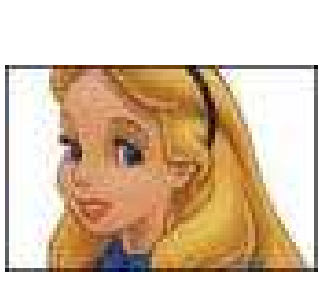
Simple Example

Day After



Simple Example

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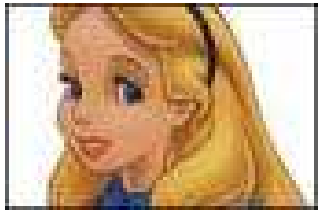
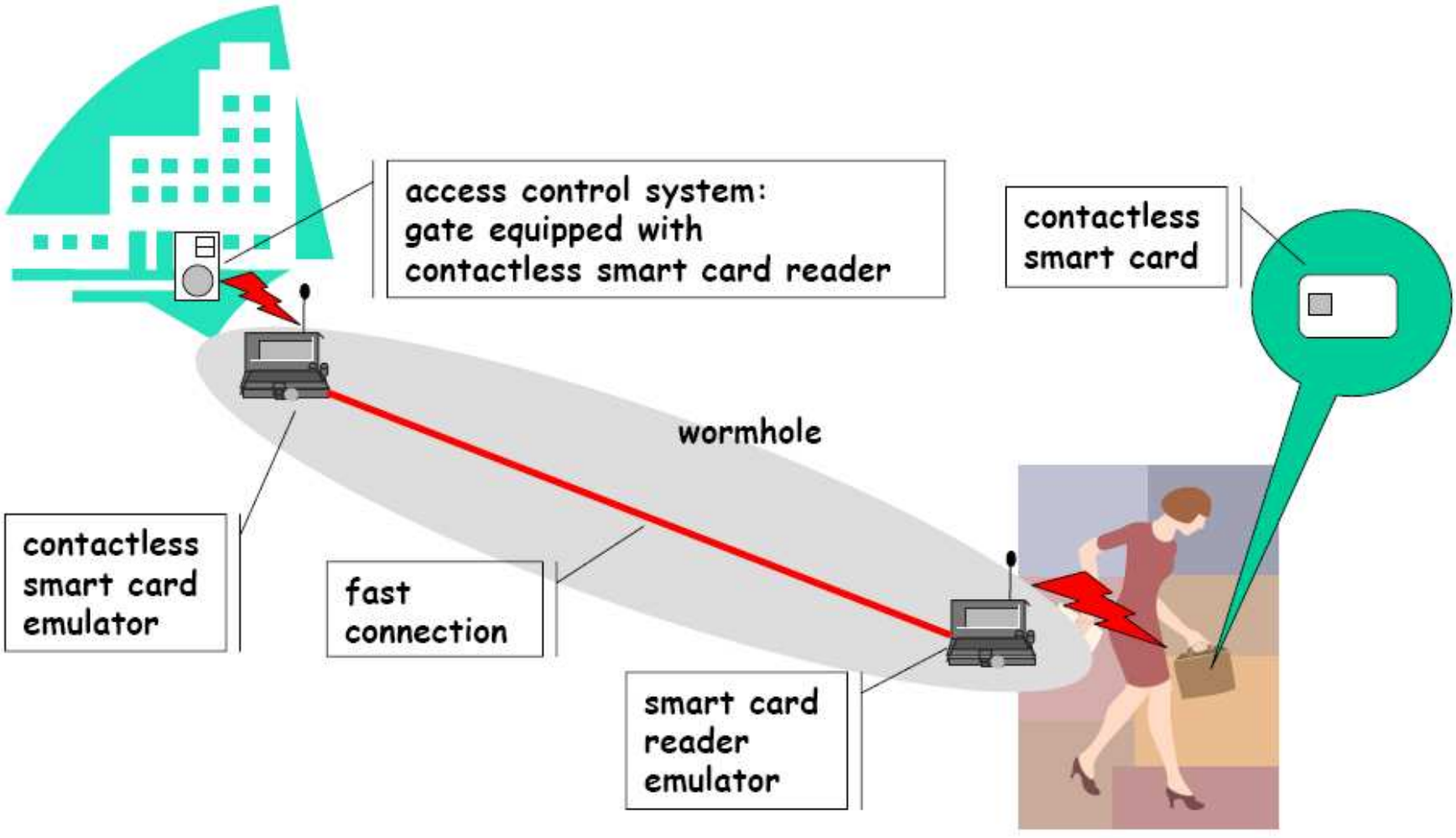
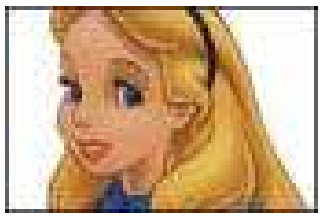


This kind of attack is valid for all encryptions

Authentication Problem: Wormhole Attack



Example: Needham-Schroeder Protocol 1978



$\longrightarrow \quad \{A, N_A\}_{K_B} \quad \longrightarrow$

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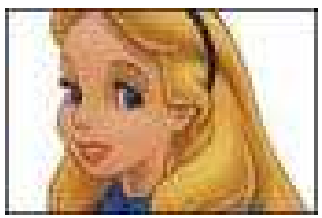

$\longrightarrow \quad \{A, N_A\}_{K_B} \quad \longrightarrow$

$\longleftarrow \quad \{N_A, N_B\}_{K_A} \quad \longleftarrow$

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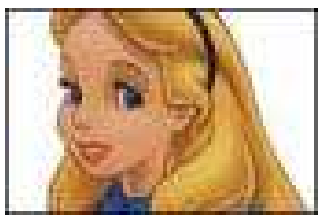

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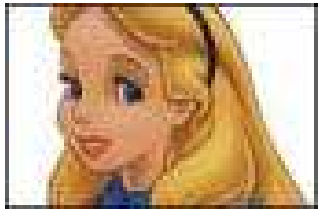
Question

- Is N_B a shared secret between A et B?

Example: Needham-Schroeder Protocol 1978



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$\longrightarrow \quad \{N_B\}_{K_B} \quad \longrightarrow$

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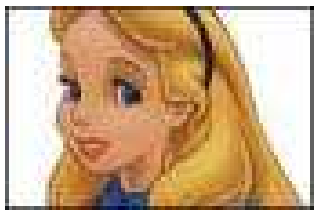
- Is N_B a shared secret between A et B?

Answer

- In 1995, G.Lowe find an attack 17 years after its publication!

Lowe Attack on the Needham-Schroeder

so-called "Man in the middle attack"



Agent A

Intruder I

Agent B

$$
\begin{array}{lcll}
A & \longrightarrow & B & : \{A, N_a\}_{K_B} \\
B & \longrightarrow & A & : \{N_a, N_b\}_{K_A} \\
A & \longrightarrow & B & : \{N_b\}_{K_B}
\end{array}
$$

Lowe Attack on the Needham-Schroeder

so-called "Man in the middle attack"

$\{A, N_a\}_{K_I}$

Agent A Intruder I Agent B

- $A \longrightarrow B : \{A, N_a\}_{K_B}$
  $B \longrightarrow A : \{N_a, N_b\}_{K_A}$
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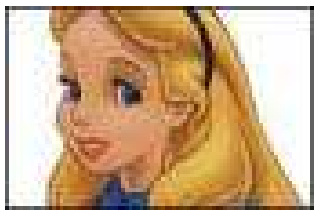

$\{A, N_a\}_{K_I}$ →

$\{A, N_a\}_{K_B}$ →

Agent A Intruder I Agent B

- $A \longrightarrow B : \{A, N_a\}_{K_B}$
  $B \longrightarrow A : \{N_a, N_b\}_{K_A}$
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so-called "Man in the middle attack"

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$\{A, N_a\}_{K_B}$

$\{N_a, N_b\}_{K_A}$

Agent A Intruder I Agent B

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$\{A, N_a\}_{K_I}$ →

← $\{N_a, N_b\}_{K_A}$

$\{A, N_a\}_{K_B}$ →

← $\{N_a, N_b\}_{K_A}$

Agent A Intruder I Agent B

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Lowe Attack on the Needham-Schroeder

so-called "Man in the middle attack"

$\{A, N_a\}_{K_I}$

$\{N_a, N_b\}_{K_A}$

$\{N_b\}_{K_I}$

$\{A, N_a\}_{K_B}$

$\{N_a, N_b\}_{K_A}$

Agent A | Intruder I | Agent B

- $A \longrightarrow B : \{A, N_a\}_{K_B}$
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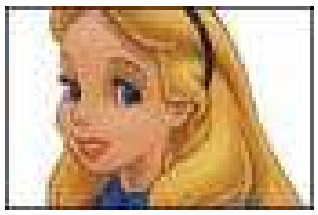

$\{A, N_a\}_{K_I}$ →
$\{N_a, N_b\}_{K_A}$ ←
$\{N_b\}_{K_I}$ →

$\{A, N_a\}_{K_B}$ →
$\{N_a, N_b\}_{K_A}$ ←
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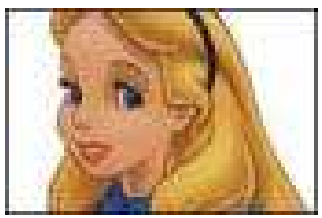
Agent A — Intruder I — Agent B

$$
\begin{array}{rccl}
 & A & \longrightarrow & B : \{A, N_a\}_{K_B} \\
 & B & \longrightarrow & A : \{N_a, N_b\}_{K_A} \\
\bullet & A & \longrightarrow & B : \{N_b\}_{K_B}
\end{array}
$$

Needham-Schroeder corrected by Lowe 1995

$\longrightarrow \quad \{A, N_A\}_{K_B} \quad \longrightarrow$

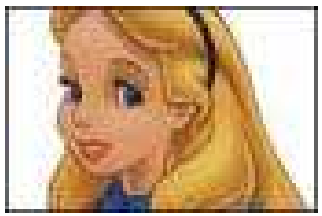
Needham-Schroeder corrected by Lowe 1995



$\longrightarrow \quad \{A, N_A\}_{K_B} \quad \longrightarrow$

$\longleftarrow \quad \{N_A, N_B, B\}_{K_A} \quad \longleftarrow$

Needham-Schroeder corrected by Lowe 1995



$\longrightarrow \quad \{A, N_A\}_{K_B} \quad \longrightarrow$

$\longleftarrow \quad \{N_A, N_B, B\}_{K_A} \quad \longleftarrow$

$\longrightarrow \quad \{N_B\}_{K_B} \quad \longrightarrow$

Needham-Schroeder corrected by Lowe 1995

$$\longrightarrow \quad \{A, N_A\}_{K_B} \quad \longrightarrow$$

$$\longleftarrow \quad \{N_A, N_B, B\}_{K_A} \quad \longleftarrow$$

$$\longrightarrow \quad \{N_B\}_{K_B} \quad \longrightarrow$$

Question

- This time the protocol is secure?

Outline

Motivations

Two Examples

History of Cryptography

Cryptographic Security Intuitions

Logical Attacks

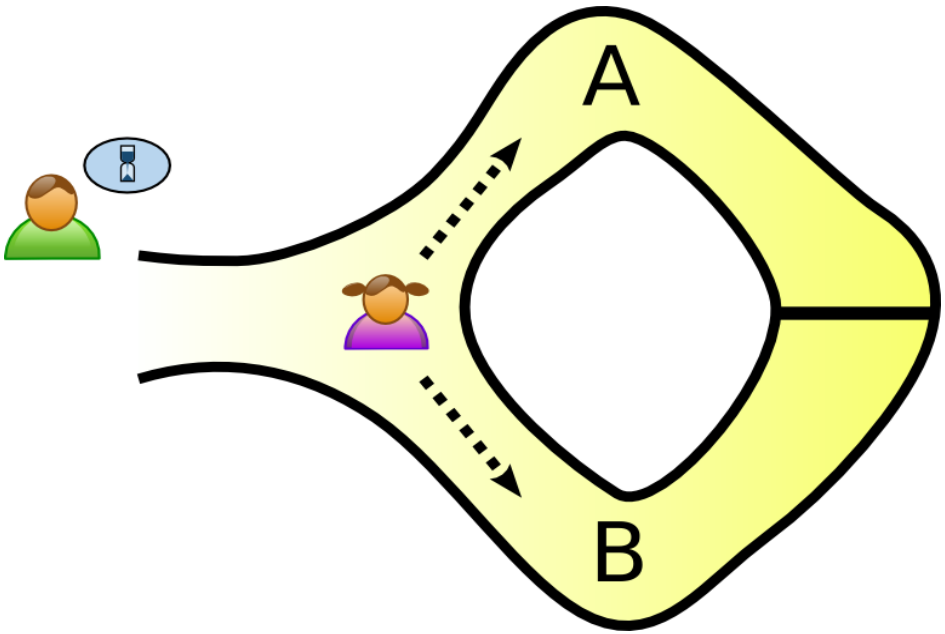
Interactive Zero Knowledge Proofs

Secret Sharing

Conclusion

Interactive Zero Knowledge Proofs

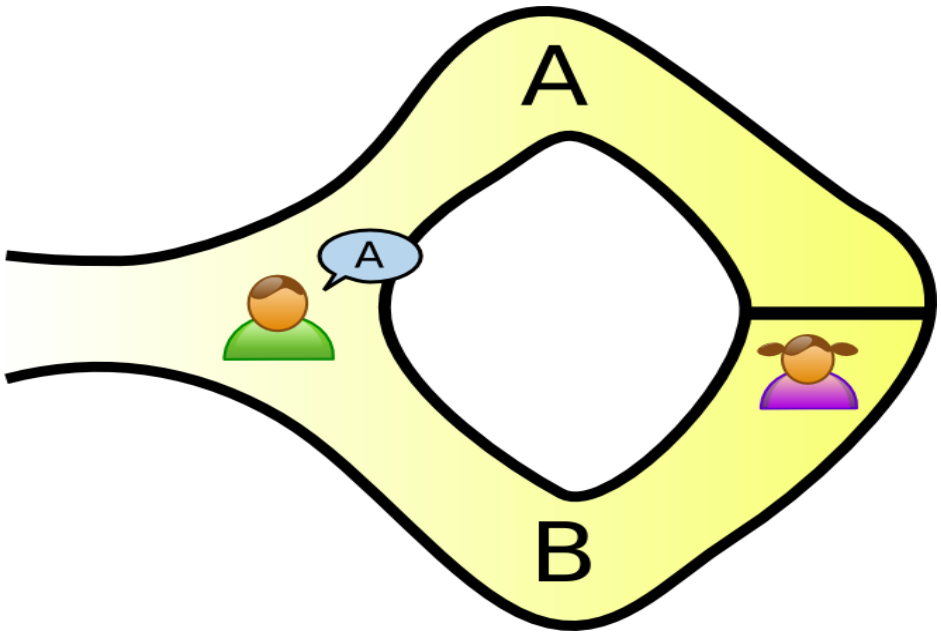
An Example: The Cave Story (2)



First, Victor waits outside while Peggy chooses a path.

Interactive Zero Knowledge Proofs

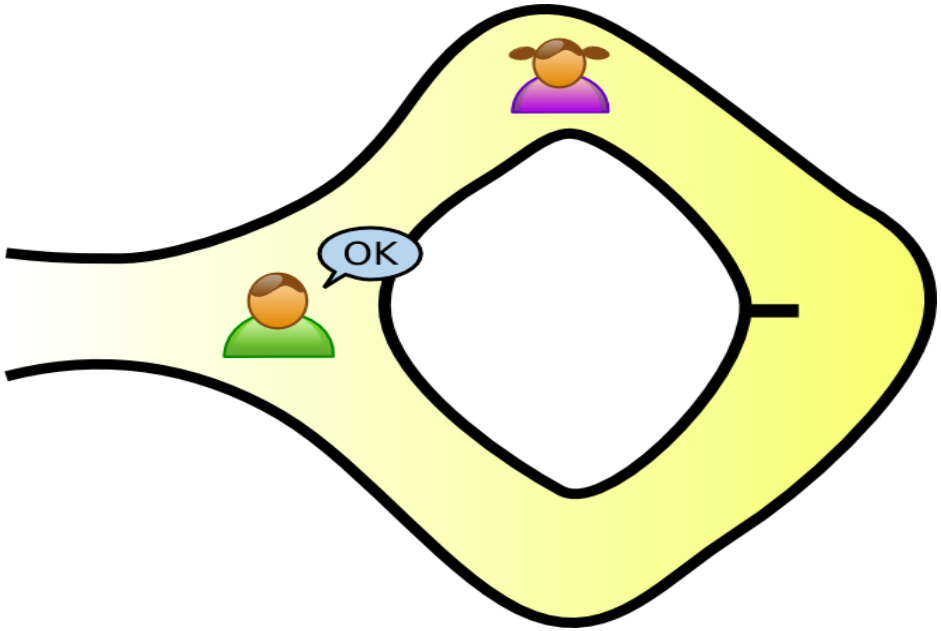
An Example: The Cave Story (3)



Then Victor enters and shouts the name of a path.

Interactive Zero Knowledge Proofs

An Example: The Cave Story (4)



At last, Peggy returns along the desired path (using the secret if necessary).

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Secret Sharing

- How keep nuclear code secret in British Army?

Secret Sharing

- How keep nuclear code secret in British Army?
- Burn it, but do not preseve integrity

How to Share a Secret Code I

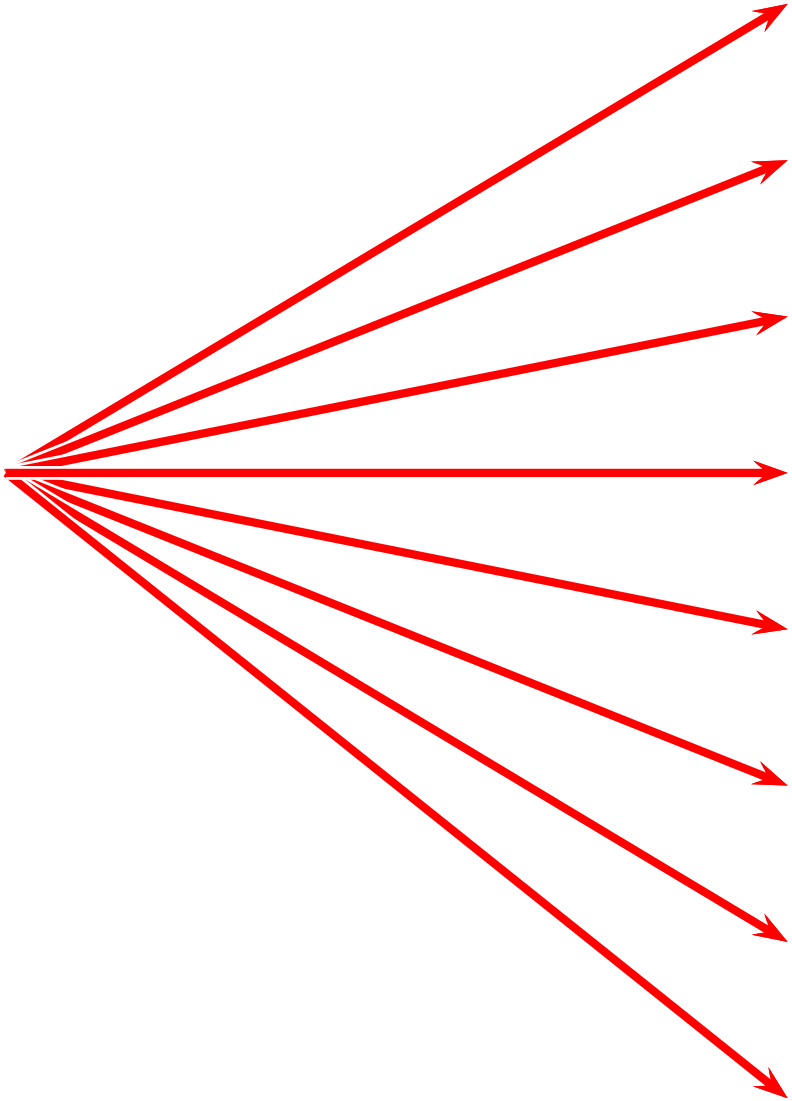
1234567

How to Share a Secret Code I

1234567

Problem of Integrity and Confidentiality

How to Share a Secret Code II



1234567

1234567

1234567

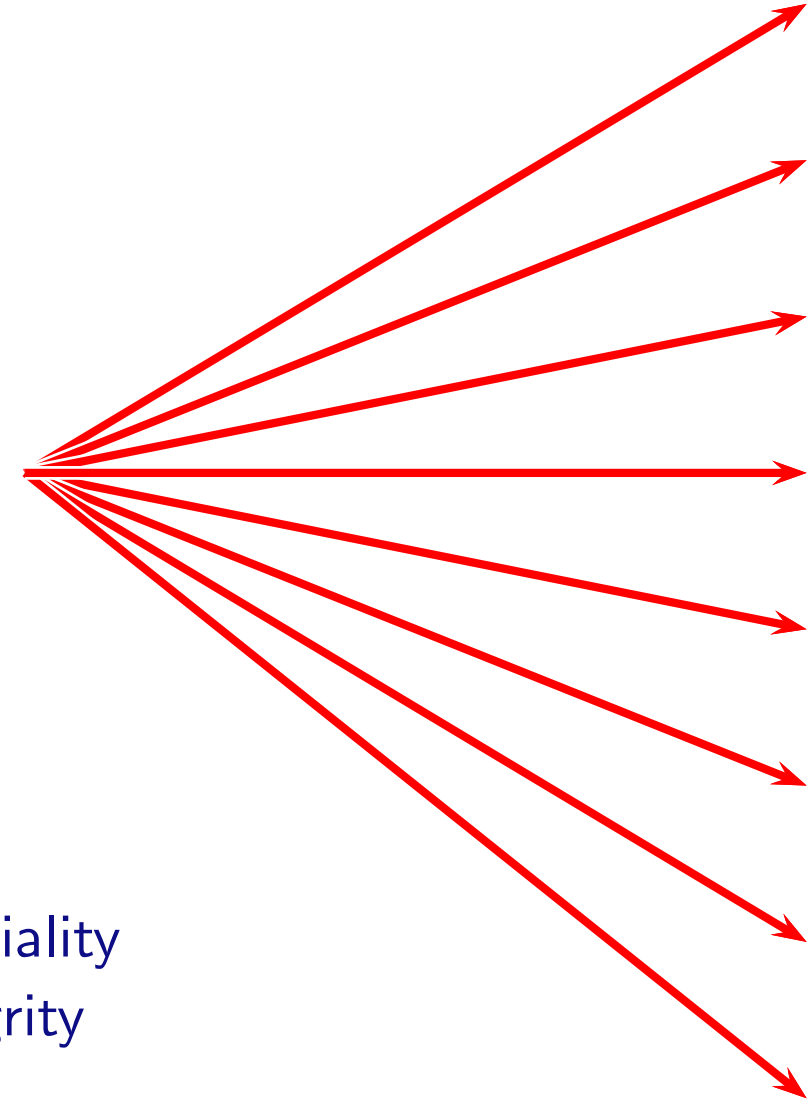
1234567

1234567

1234567

1234567

How to Share a Secret Code II



1234567

1234567

1234567

1234567

1234567

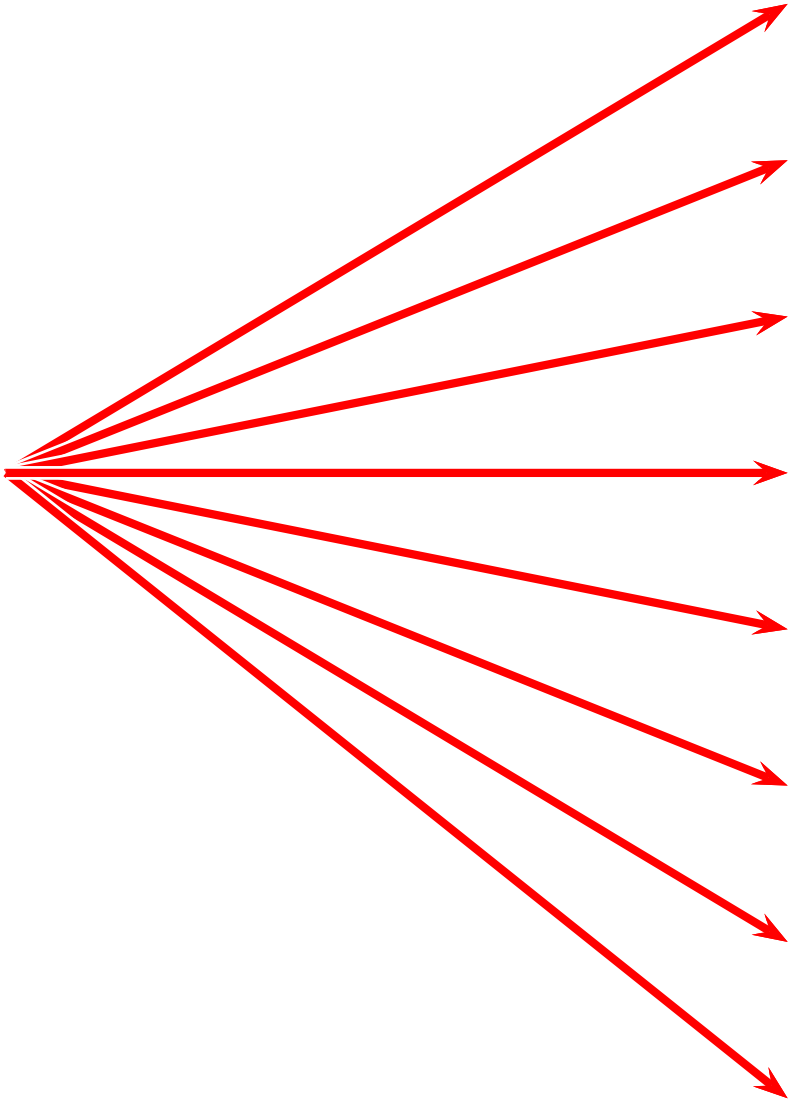
1234567

1234567

Problem of Confidentiality

No problem of Integrity

How to Share a Secret Code II



23572

11567

734567

534567

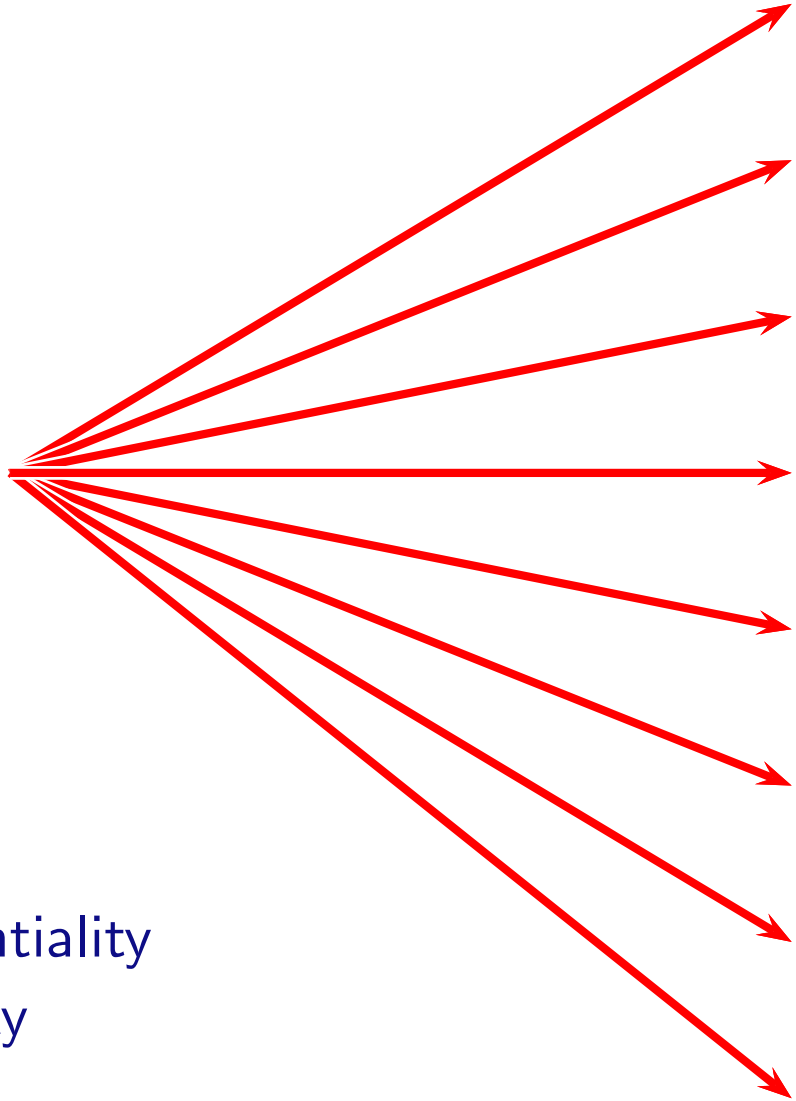
934567

563317

114567

455567

How to Share a Secret Code II



23572

11567

734567

534567

934567

563317

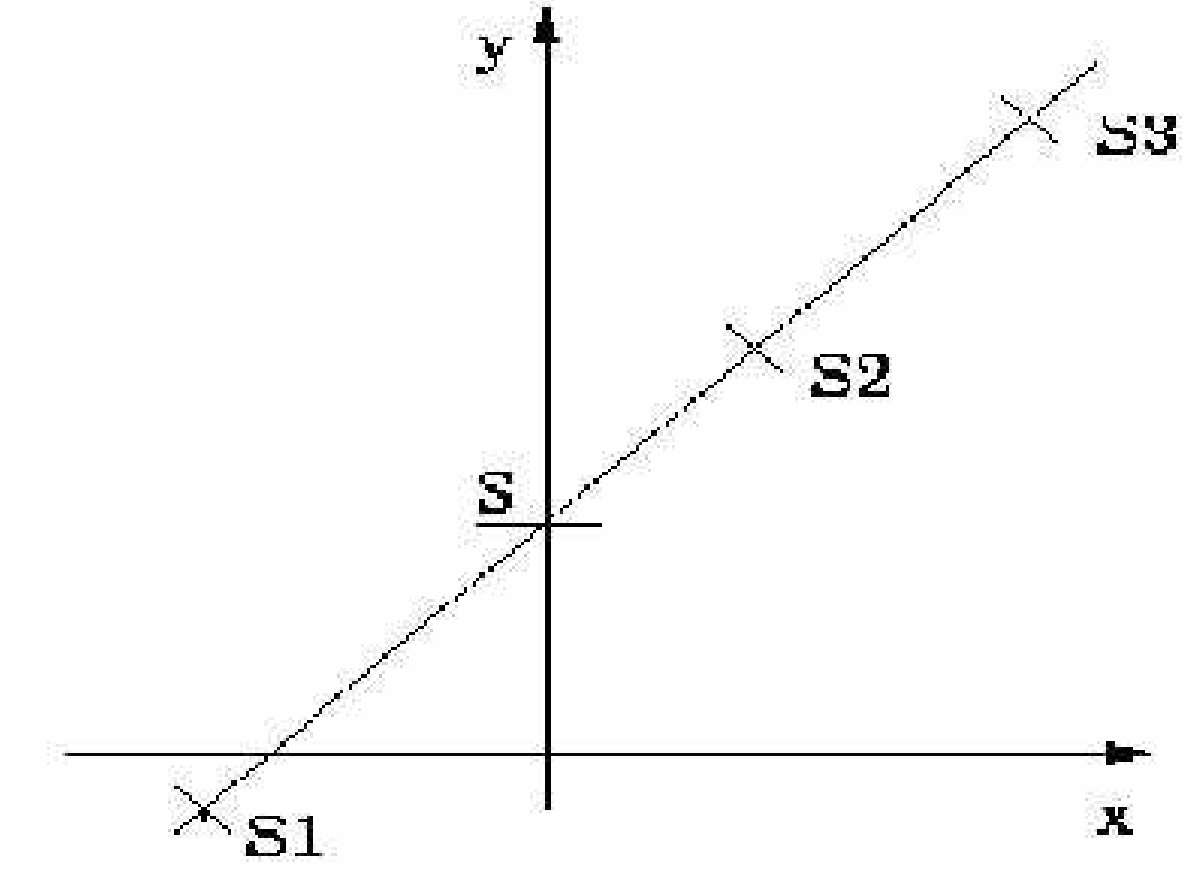
114567

455567

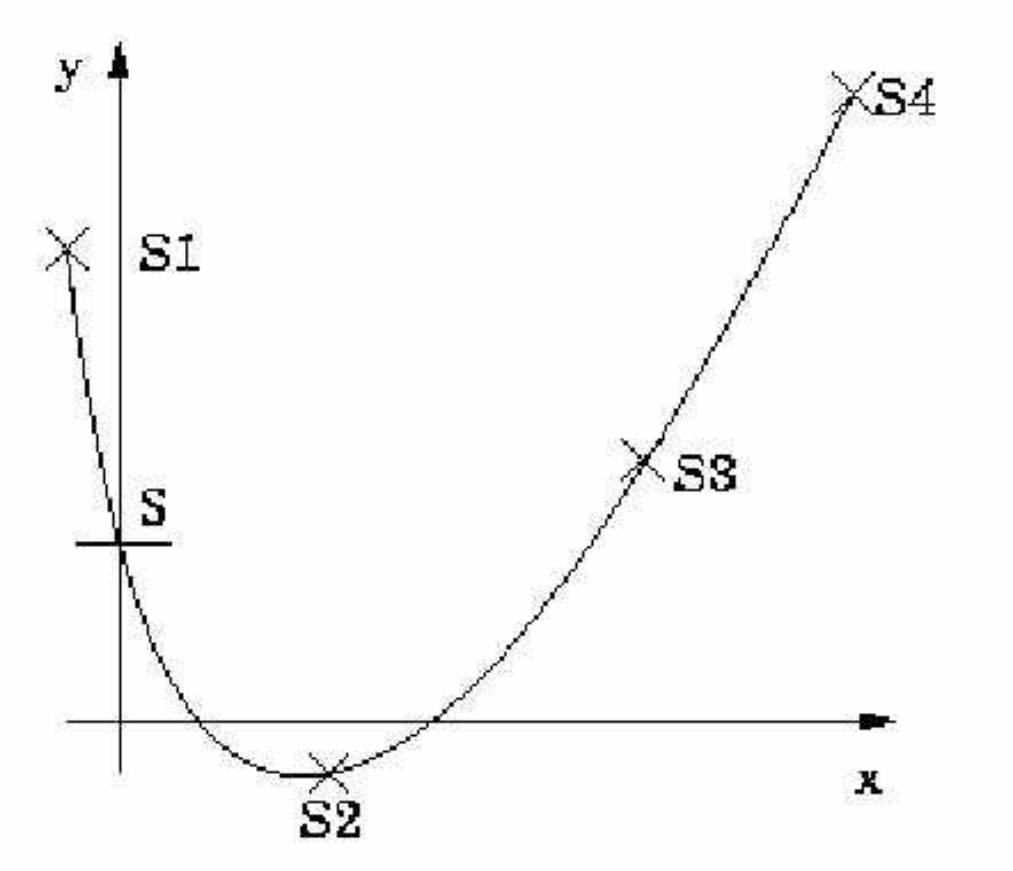
No Problem of Confidentiality

Problem of Integrity

(2,5)



(3,5)



Outline

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Summary

Today

- Motivation
- History of Cryptography
- Securities notions
- Logical attacks
- Zero - knowledge
- Secret Sharing

Thank you for your attention

Questions ?

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