

Formal Analysis of Electronic Exams

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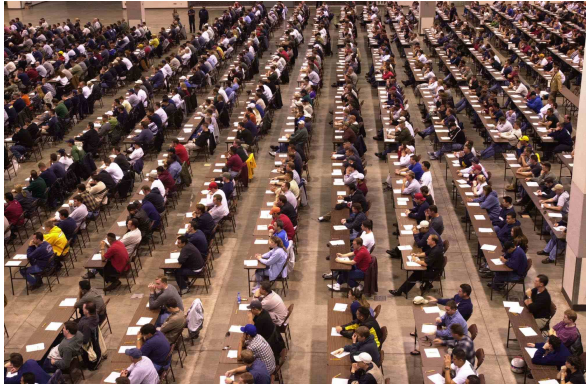
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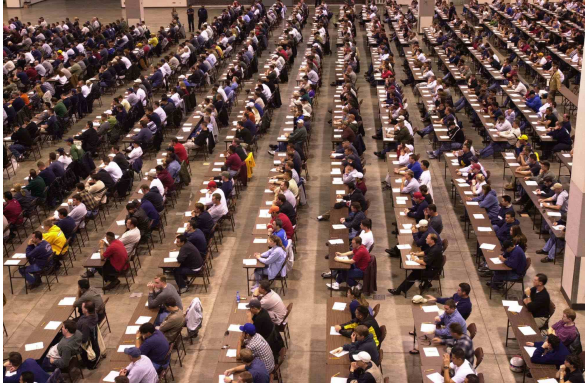
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(SECRYPT 2014), Vienna

August 28, 2014

E-exam





Information technology for the assessment of knowledge and skills.

coursera

U
UDACITY

edX

IELTSTM
English for International Opportunity



TOEFL[®]**iBT**

E-exam: Players and Organization

Three Roles:

Candidate



Examination Authority



Examiner



E-exam: Players and Organization

Three Roles:

Candidate



Examination Authority



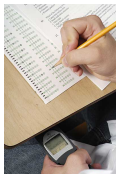
Examiner



Four Phases:

1. Registration
2. Examination
3. Marking
4. Notification

Threats...



- ▶ Candidate cheating
- ▶ Bribed, corrupted or unfair examiners
- ▶ Dishonest/untrusted exam authority
- ▶ Outside attackers
- ▶ ...

... and their Mitigation

Most existing e-exam systems assume **trusted authorities** and focus on **student cheating**:

- ▶ Exam centers
- ▶ Software solutions, e.g. ProctorU



ProctorU
*Real People.
Real Proctoring.*

... and their Mitigation

Most existing e-exam systems assume **trusted authorities** and focus on **student cheating**:

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Yet also the **other threats** are real:

- ▶ Atlanta Public Schools cheating scandal (2009)
- ▶ UK student visa tests fraud (2014)

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⇒ need for better protocols and systems (cf. case studies)

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- ▶ UK student visa tests fraud (2014)

So what about **dishonest authorities** or **hackers** attacking the system?

- ⇒ need for better protocols and systems (cf. case studies)
- ⇒ **precise formal definitions of required properties**

Introduction

Model and Properties

- Authentication Properties

- Privacy Properties

Case Studies

- Huszti & Pethő's Protocol

- Remark! Protocol

Conclusion

Introduction

Model and Properties

- Authentication Properties

- Privacy Properties

Case Studies

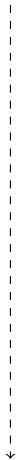
- Huszti & Pethő's Protocol

- Remark! Protocol

Conclusion

- ▶ **Processes** in the applied π -calculus [?]
- ▶ Annotated using **events**
- ▶ **Authentication** properties as **correspondence** between events
- ▶ **Privacy** properties as **observational equivalence** between instances
- ▶ **Automatic** verification using ProVerif [?]

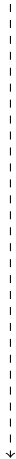
Model



Model



1. Registration




Model



1. Registration

Register

reg()



Model

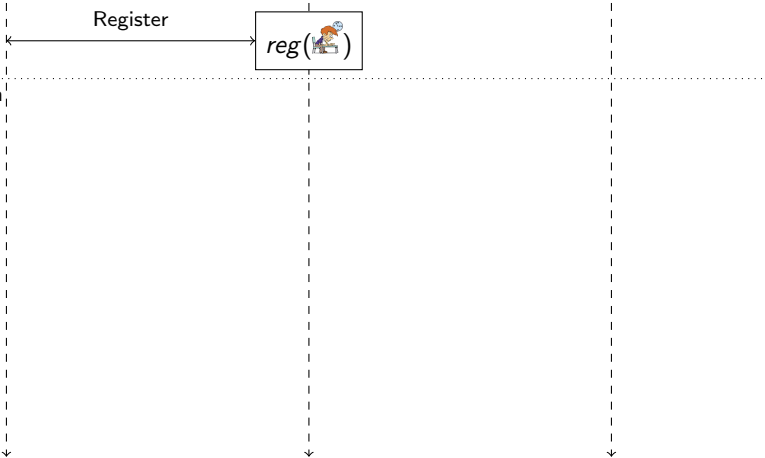


1. Registration

Register

reg()

2. Examination



Model



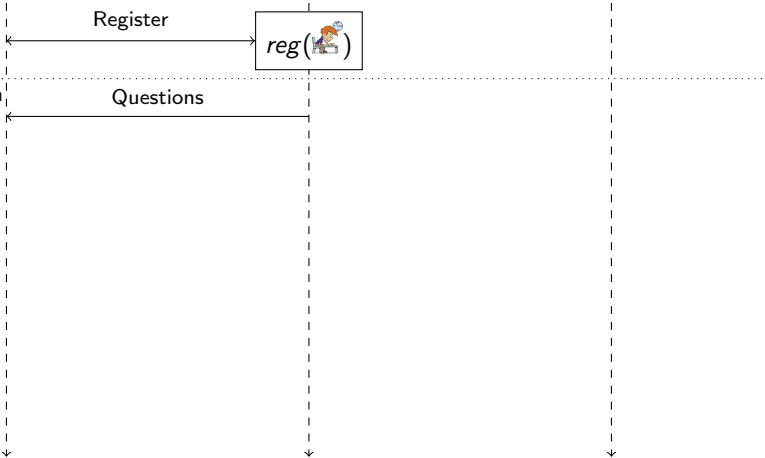
1. Registration

Register



2. Examination

Questions

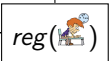


Model



1. Registration

Register

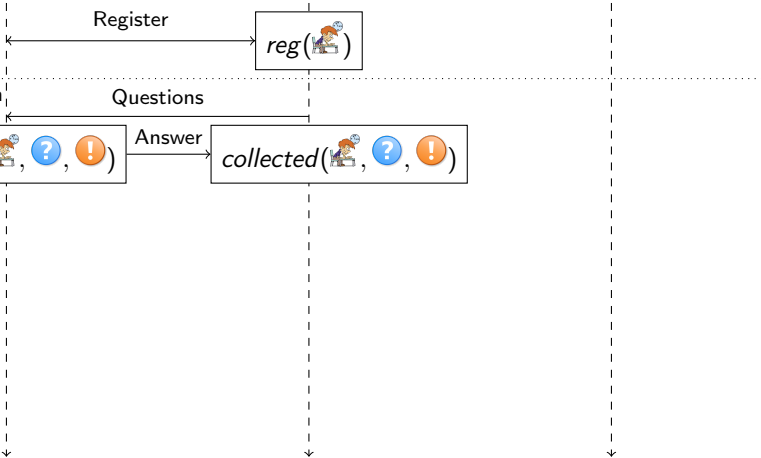


2. Examination

Questions



Answer

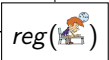


Model



1. Registration

Register



2. Examination

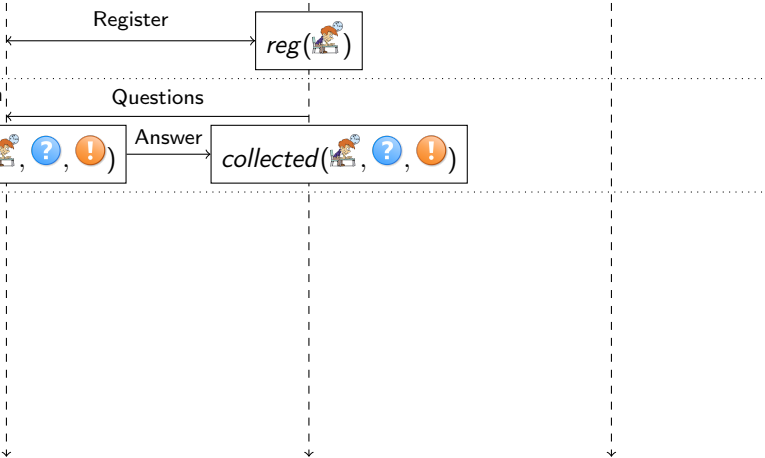
Questions



Answer



3. Marking

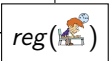


Model



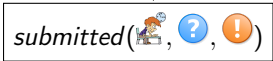
1. Registration

Register

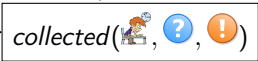


2. Examination

Questions

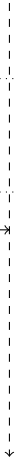


Answer



3. Marking

Form



Model



1. Registration

Register

reg()

2. Examination

Questions

Answer

submitted(, , )

collected(, , )

3. Marking

Form

distrib(, , , , )

Mark

marked(, , , , )

Model



1. Registration

Register

reg()

2. Examination

Questions

submitted(, , )

Answer

collected(, , )

3. Marking

distrib(, , , , )

Form

Mark

marked(, , , , )

4. Notification

Model



1. Registration

Register

reg()

2. Examination

Questions

submitted(, , )

Answer

collected(, , )

3. Marking

distrib(, , , , )

Form

Mark

marked(, , , , )

4. Notification

notified(, )

Mark

Introduction

Model and Properties

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- Huszti & Pethő's Protocol

- Remark! Protocol

Conclusion

Answer Origin Authentication

All collected answers originate from registered candidates, and only one answer per candidate is accepted.


Definition:

On every trace:



1. Registration



Register

`reg()`

2. Examination

Questions

preceded by distinct occurrence

`submitted(, , )`

Answer

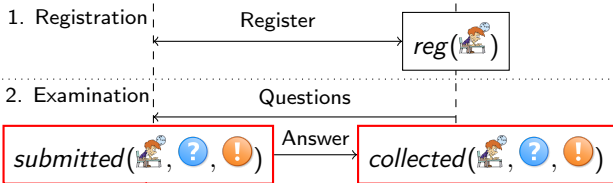
`collected(, , )`

Form Authorship

Answers are collected as submitted, i.e. without modification.

Definition:

On every trace:



preceded by distinct occurrence

Form Authenticity

Answers are marked as collected.

Definition:

On every trace:



2. Examination

Questions

`submitted(👤, ?, !)`

Answer

`collected(👤, ?, !)`

3. Marking

`distrib(👤, ?, !, 📄, 🐻)`

Form

Mark

`marked(?, !, 📄, A+, 🐻)`

preceded by dist. occ.

Mark Authenticity

The candidate is notified with the mark associated to his answer.

Definition:

On every trace:



3. Marking



Form

4. Notification



Mark



Mark

preceded by distinct occurrence

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Remark! Protocol

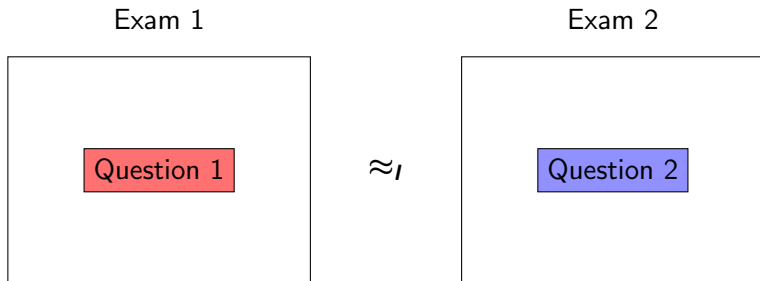
Conclusion

Question Indistinguishability

No premature information about the questions is leaked.

Definition:

Observational equivalence of two instances up to the end of registration phase:

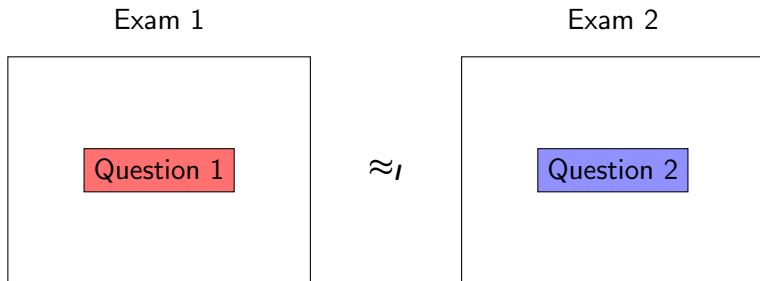


Question Indistinguishability

No premature information about the questions is leaked.

Definition:

Observational equivalence of two instances up to the end of registration phase:



Can be considered with or without dishonest candidates.

Anonymous Marking

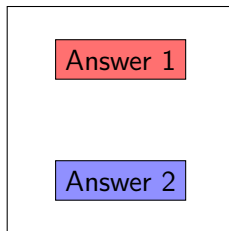
An examiner cannot link an answer to a candidate.

Definition:

Up to the end of marking phase:

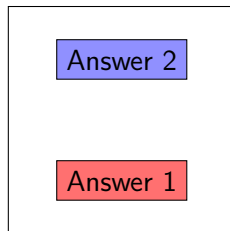


Exam 1



\approx

Exam 2

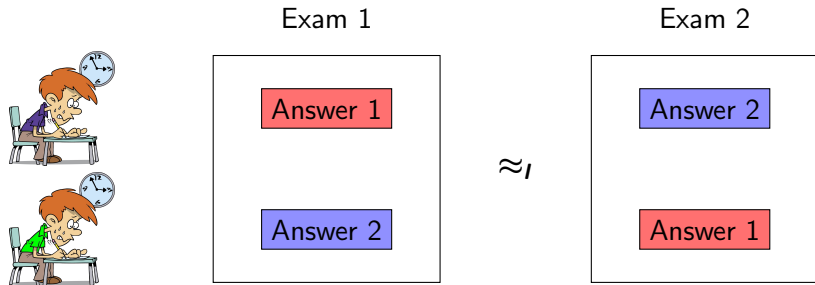


Anonymous Marking

An examiner cannot link an answer to a candidate.

Definition:

Up to the end of marking phase:

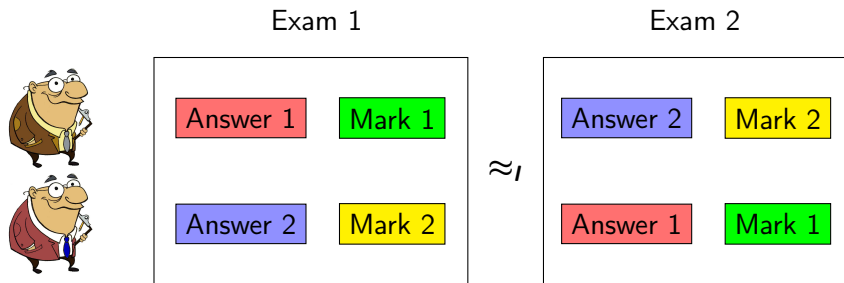


Can be considered with or without dishonest examiners and authorities.

Anonymous Examiner

A candidate cannot know which examiner graded his copy.

Definition:



Can be considered with or without dishonest candidates.

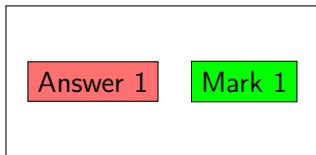
Mark Privacy

Marks are private.

Definition:

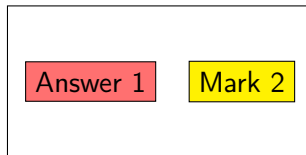


Exam 1



\approx

Exam 2

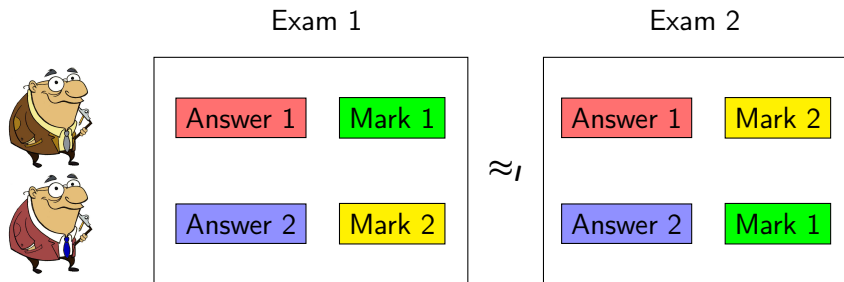


Can be considered with or without dishonest candidates, examiners and authorities.

Mark Anonymity

Marks can be published, but may not be linked to candidates.

Definition:



Can be considered with or without dishonest candidates, examiners and authorities.

Implied by Mark Privacy.

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“A Secure Electronic Exam System” [?] using

- ▶ ElGamal Encryption
- ▶ a Reusable Anonymous Return Channel (RARC) [?] for **anonymous communication**
- ▶ a network of servers providing a timed-release service using Shamir's Secret Sharing:
A subset of servers can combine their shares to **de-anonymize a candidate** after the exam

Goal: ensure

- ▶ authentication and privacy

in presence of **dishonest**

- ▶ candidates
- ▶ examiners
- ▶ exam authorities

Formal Verification with ProVerif [?]:

Property	Result	Time
Answer Origin Authentication	×	< 1 s
Form Authorship	×	< 1 s
Form Authenticity	×	< 1 s
Mark Authenticity	×	< 1 s
Question Indistinguishability	×	< 1 s
Anonymous Marking	×	8 m 46 s
Anonymous Examiner	×	9 m 8 s
Mark Privacy	×	39 m 8 s
Mark Anonymity	×	1h 15 m 58 s

Given its security definition, the **RARC**

- ▶ provides anonymity, but not necessarily secrecy
- ▶ does not necessarily provide integrity or authentication
- ▶ is only secure against **passive attackers**

Corrupted parties or active attackers can **break secrecy and anonymity**, as the following attack shows.

RARC: Mode of Operation and Attack

Input (A to RARC, destination B):

$\{ID_A, PK_A\}_{PK_{RARC}} + PoK; \{MSG\}_{PK_{RARC}}; \{ID_B, PK_B\}_{PK_{RARC}} + PoK$

RARC: Mode of Operation and Attack

Input (A to RARC, destination B):

$\{ID_A, PK_A\}_{PK_{RARC}} + PoK; \{MSG\}_{PK_{RARC}}; \{ID_B, PK_B\}_{PK_{RARC}} + PoK$

Output (RARC to B):

$\{ID_A, PK_A\}_{PK_{RARC}} + Signature; \{MSG\}_{PK_B}$

RARC: Mode of Operation and Attack

Input (A to RARC, destination B):

$\{ID_A, PK_A\}_{PK_{RARC}} + PoK; \{MSG\}_{PK_{RARC}}; \{ID_B, PK_B\}_{PK_{RARC}} + PoK$

Output (RARC to B):

$\{ID_A, PK_A\}_{PK_{RARC}} + Signature; \{MSG\}_{PK_B}$

Return (B to RARC, destination A):

$\{ID_B, PK_B\}_{PK_{RARC}} + PoK; \{MSG\}_{PK_{RARC}}; \{ID_A, PK_A\}_{PK_{RARC}} + Signature$

RARC: Mode of Operation and Attack

Input (A to RARC, destination B):

$\{ID_A, PK_A\}_{PK_{RARC}} + PoK; \{MSG\}_{PK_{RARC}}; \{ID_B, PK_B\}_{PK_{RARC}} + PoK$

Output (RARC to B):

$\{ID_A, PK_A\}_{PK_{RARC}} + Signature; \{MSG\}_{PK_B}$

Return (B to RARC, destination A):

$\{ID_B, PK_B\}_{PK_{RARC}} + PoK; \{MSG\}_{PK_{RARC}}; \{ID_A, PK_A\}_{PK_{RARC}} + Signature$

Attack

Input (AD to RARC, destination AD):

$\{ID_{AD}, PK_{AD}\}_{PK_{RARC}} + PoK; \{MSG\}_{PK_{RARC}}; \{ID_{AD}, PK_{AD}\}_{PK_{RARC}} + PoK$

RARC: Mode of Operation and Attack

Input (A to RARC, destination B):

$\{ID_A, PK_A\}_{PK_{RARC}} + PoK; \{MSG\}_{PK_{RARC}}; \{ID_B, PK_B\}_{PK_{RARC}} + PoK$

Output (RARC to B):

$\{ID_A, PK_A\}_{PK_{RARC}} + Signature; \{MSG\}_{PK_B}$

Return (B to RARC, destination A):

$\{ID_B, PK_B\}_{PK_{RARC}} + PoK; \{MSG\}_{PK_{RARC}}; \{ID_A, PK_A\}_{PK_{RARC}} + Signature$

Attack

Input (AD to RARC, destination AD):

$\{ID_{AD}, PK_{AD}\}_{PK_{RARC}} + PoK; \{MSG\}_{PK_{RARC}}; \{ID_{AD}, PK_{AD}\}_{PK_{RARC}} + PoK$

Output (RARC to AD):

$\{ID_{AD}, PK_{AD}\}_{PK_{RARC}} + Signature; \{MSG\}_{PK_{AD}}$

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Application: Remark! Protocol

A recent protocol [?] using

- ▶ ElGamal encryption
- ▶ an **exponentiation mixnet** [?] to create **pseudonyms** based on the parties' public keys
⇒ allows to encrypt and sign anonymously
- ▶ a public append-only **bulletin board**

Goal: ensure

- ▶ authentication and integrity
- ▶ privacy
- ▶ verifiability

in presence of **dishonest**

- ▶ candidates
- ▶ examiners
- ▶ exam authorities

Formal Verification with ProVerif:

Property	Result	Time
Answer Origin Authentication	✓	< 1 s
Form Authorship	✓	< 1 s
Form Authenticity	✓ ¹	< 1 s
Mark Authenticity	✓	< 1 s
Question Indistinguishability	✓	< 1 s
Anonymous Marking	✓	2 s
Anonymous Examiner	✓	1 s
Mark Privacy	✓	3 m 32 s
Mark Anonymity	✓	- ²

¹after fix

²implied by Mark Privacy

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Conclusion

- ▶ **E-exams** are used and vulnerable to attacks
- ▶ Cryptographic protocols exist, but **lack formal verification**
- ▶ **First formal framework** for analysis of e-exams:
 - ▶ Formal model in the **applied π -calculus**
 - ▶ **Definitions** for central authentication, integrity and privacy properties
- ▶ **Automated verification in ProVerif** of two case studies:
 - ▶ Huszti & Pethő's protocol: Fails on all properties due to severe flaws in protocol design
 - ▶ Remark! protocol: Ensures all properties after one fix
- ▶ **Future work:** verifiability and accountability, analyzing implementations

Thank you for your attention!

Questions?

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Definition

(E-exam protocol). *An e-exam protocol is a tuple*

$$(C, E, Q, A_1, \dots, A_l, \tilde{n}_p),$$

where

- ▶ *C is the process executed by the candidates,*
- ▶ *E is the process executed by the examiners,*
- ▶ *Q is the process executed by the question committee,*
- ▶ *A_i's are the processes executed by the authorities, and*
- ▶ *\tilde{n}_p is the set of private channel names.*

Definition

(E-exam instance). *An e-exam instance is a closed process*

$$EP = \nu \tilde{n}. (C\sigma_{id_1}\sigma_{a_1} | \dots | C\sigma_{id_j}\sigma_{a_j} | E\sigma_{id'_1}\sigma_{m_1} | \dots | E\sigma_{id'_k}\sigma_{m_k} | Q\sigma_q | A_1\sigma_{dist} | \dots | A_l),$$

where

- ▶ \tilde{n} is the set of all restricted names, which includes the set of the protocol's private channels;
- ▶ $C\sigma_{id_i}\sigma_{a_i}$'s are the processes run by the candidates, the substitutions σ_{id_i} and σ_{a_i} specify the identity and the answers of the i^{th} candidate respectively;
- ▶ $E\sigma_{id'_i}\sigma_{m_i}$'s are the processes run by the examiners, the substitution $\sigma_{id'_i}$ specifies the i^{th} examiner's identity, and σ_{m_i} specifies for each possible question/answer pair the corresponding mark;

Definition

(E-exam instance). An e-exam instance is a closed process

$$EP = \nu \tilde{n}. (C\sigma_{id_1}\sigma_{a_1} | \dots | C\sigma_{id_j}\sigma_{a_j} | E\sigma_{id'_1}\sigma_{m_1} | \dots | E\sigma_{id'_k}\sigma_{m_k} | Q\sigma_q | A_1\sigma_{dist} | \dots | A_l),$$

where

- ▶ Q is the process run by the question committee, the substitution σ_q specifies the exam questions;
- ▶ the A_i 's are the processes run by the exam authorities, the substitution σ_{dist} determines which answers will be submitted to which examiners for grading.

Without loss of generality, we assume that A_1 is in charge of distributing the copies to the examiners.

Definition (Answer Origin Authentication)

An e-exam protocol ensures Answer Origin Authentication if, for every e-exam process EP , each occurrence of the event **collected**($id_c, ques, ans$) is **preceded** by a distinct occurrence of the event **reg**(id_c) on every execution trace.

Definition (Form Authorship)

An e-exam protocol ensures Form Authorship if, for every e-exam process EP , each occurrence of the event **collected**($id_c, ques, ans$) is **preceded** by a distinct occurrence of the event **submitted**($id_c, ques, ans$) on every execution trace.

Definition (Form Authenticity)

An e-exam protocol ensures Form Authenticity if, for every e-exam process EP , each occurrence of the event $\mathit{marked}(ques, ans, mark, id_form, id_e)$ is preceded by a distinct occurrence of the events $\mathit{distrib}(id_c, ques, ans, id_form, id_e)$ and $\mathit{collected}(id_c, ques, ans)$ on every execution trace.

Definition (Mark Authenticity)

An e-exam protocol ensures Mark Authenticity if, for every e-exam process EP , each occurrence of the event $\mathit{notified}(id_c, mark)$ is preceded by a distinct occurrence of the events $\mathit{marked}(ques, ans, mark, id_form, id_e)$ and $\mathit{distrib}(id_c, ques, ans, id_form, id_e)$ on every execution trace.

Definition (Question Indistinguishability)

An e-exam protocol ensures Question Indistinguishability if for any e-exam process EP that ends with the registration phase, any questions q_1 and q_2 , we have that:

$$EP_{\{id_Q\}}[Q\sigma_{q_1}]|_{reg} \approx_I EP_{\{id_Q\}}[Q\sigma_{q_2}]|_{reg}.$$

Definition (Anonymous Marking)

An e-exam protocol ensures Anonymous Marking if for any e-exam process EP that ends with the marking phase, any two candidates id_1 and id_2 , and any two answers a_1 and a_2 , we have that:

$$EP_{\{id_1, id_2\}}[C\sigma_{id_1}\sigma_{a_1} | C\sigma_{id_2}\sigma_{a_2}]|_{mark} \approx_I \\ EP_{\{id_1, id_2\}}[C\sigma_{id_1}\sigma_{a_2} | C\sigma_{id_2}\sigma_{a_1}]|_{mark}.$$

Definition (Anonymous Examiner)

An e-exam protocol ensures Anonymous Examiner if for any e-exam process EP , any two candidates id_1, id_2 ,

any two examiners id'_1, id'_2 , and any two marks m_1, m_2 , we have that:

$$EP_{\{id_1, id_2, id'_1, id'_2, id_{A_1}\}} [C\sigma_{id_1}\sigma_{a_1} | C\sigma_{id_2}\sigma_{a_2} | E\sigma_{id'_1}\sigma_{m_1} | E\sigma_{id'_2}\sigma_{m_2} | A_1\sigma_{dist_1}] \approx_I \\ EP_{\{id_1, id_2, id'_1, id'_2, id_{A_1}\}} [C\sigma_{id_1}\sigma_{a_1} | C\sigma_{id_2}\sigma_{a_2} | E\sigma_{id'_1}\sigma_{m_2} | E\sigma_{id'_2}\sigma_{m_1} | A_1\sigma_{dist_2}]$$

where σ_{dist_1} attributes the exam form of candidate id_1 to examiner id'_1 and the exam form of candidate id_2 to examiner id'_2 , and σ_{dist_2} attributes the exam form of candidate id_1 to examiner id'_2 and the exam form of candidate id_2 to examiner id'_1 .

Definition (Mark Privacy)

An e-exam protocol ensures Mark Privacy if for any e-exam process EP , any marks m_1, m_2 , we have that:

$$EP_{\{id'\}} [E\sigma_{id'}\sigma_{m_1}] \approx_I EP_{\{id'\}} [E\sigma_{id'}\sigma_{m_2}].$$

Definition (Mark Anonymity)

An e-exam protocol ensures Mark Anonymity if for any e-exam process EP , any candidates id_1, id_2 , any examiner id'_1 , any answers a_1, a_2 and a distribution σ_{dist} that assigns the answers of both candidates to the examiner, and two substitutions σ_{m_a} and σ_{m_b} which are identical, except that σ_{m_a} attributes the mark m_1 to the answer a_1 and m_2 to a_2 , whereas σ_{m_b} attributes m_2 to the answer a_1 and m_1 to a_2 , we have that:

$$EP_{\{id_1, id_2, id'_1, id_{A_1}\}} [C\sigma_{id_1}\sigma_{a_1} | C\sigma_{id_2}\sigma_{a_2} | E\sigma_{id'_1}\sigma_{m_a} | A_1\sigma_{dist}] \approx_I \\ EP_{\{id_1, id_2, id'_1, id_{A_1}\}} [C\sigma_{id_1}\sigma_{a_1} | C\sigma_{id_2}\sigma_{a_2} | E\sigma_{id'_1}\sigma_{m_b} | A_1\sigma_{dist}]$$

Remark! Equational Theory

$$\text{checkpseudo}(\text{pseudo_pub}(pk(k), rce), \\ \text{pseudo_priv}(k, \text{exp}(rce))) = \text{true}$$

$$\text{decrypt}(\text{encrypt}(m, pk(k), r), k) = m$$

$$\text{decrypt}(\text{encrypt}(m, \text{pseudo_pub}(pk(k), \\ rce), r), \text{pseudo_priv}(k, \text{exp}(rce)))) = m$$

$$\text{getmess}(\text{sign}(m, k)) = m$$

$$\text{checksign}(\text{sign}(m, k), pk(k)) = m$$

$$\text{checksign}(\text{sign}(m, \text{pseudo_priv}(k, \\ \text{exp}(rce))), \text{pseudo_pub}(pk(k), rce)) = m$$

Remark! Protocol

Assumption: The protocol assumes a list of eligible examiners and their public keys PK_E , and a list of eligible candidates and their public keys PK_C .

Examiner Registration

- 1- *NET* calculates $\bar{r}_e = \prod_{i=1}^k r_{e_i}$, $\overline{PK}_E = PK_E^{\bar{r}_e}$ and $h_e = g^{\bar{r}_e}$
- 2- *NET* publishes $sign((\overline{PK}_E, h_e), SK_{NET})$
- 3- *E* checks if $\overline{PK}_E = h_e^{SK_E}$

Candidate Registration

- 4- *NET* calculates $\bar{r}_c = \prod_{i=1}^k r_{c_i}$, $\overline{PK}_C = PK_C^{\bar{r}_c}$ and $h_c = g^{\bar{r}_c}$
- 5- *NET* publishes $sign((\overline{PK}_C, h_c), SK_{NET})$
- 6- *C* checks if $\overline{PK}_C = h_c^{SK_C}$

Examination

- 7- *EA* \rightarrow *C* : $\{sign(question, SK_{EA})\}_{\overline{PK}_C}$
- 8- *C* \rightarrow *EA* : $// C_a = \{question, answer, \overline{PK}_C\}$
 $\{C_a, sign(C_a, \overline{SK}_C, h_c)\}_{PK_{EA}}$
- 9- *EA* \rightarrow *C* : $\{C_a, sign(C_a, SK_{EA})\}_{\overline{PK}_C}$

Marking

10- $EA \rightarrow E : \{C_a, \text{sign}(C_a, SK_{EA})\}_{\overline{PK_E}}$

11- $E \rightarrow EA : // M_a = (\text{sign}(C_a, SK_{EA}), \text{mark})$

$\{\text{sign}(M_a, \overline{SK_E}, h_e)\}_{PK_{EA}}$

Notification

12- $EA \rightarrow C : \{M_a, \text{sign}(M_a, \overline{SK_E}, h_e)\}_{\overline{PK_C}}$

13- $NET \rightarrow EA : \{\bar{r}_c, \text{sign}(\bar{r}_c, SK_N)\}_{PK_{EA}}$

Huszti Equational Theory

$$\text{decrypt}(\text{encrypt}(m, \text{pk}(k), r), k) = m$$

$$\text{getmess}(\text{sign}(m, k)) = m$$

$$\text{checksign}(\text{sign}(m, k), \text{pk}(k)) = m$$

$$\text{exp}(\text{exp}(g, x), y) = \text{exp}(\text{exp}(g, y), x)$$

$$\text{checkproof}(\text{xproof}(p, p1, g, \text{exp}(g, e), e),$$

$$p, p1, g, \text{exp}(g, e)) = \text{true}$$

$$\text{zkpsec}(\text{zkp_proof}(\text{exp}(b, e), e), \text{exp}(b, e)) = \text{true}$$

Huszti's Protocol

Setup

- 1 - *EA* publishes g and $h = g^s$
- 2 - *Committee* \rightarrow_{priv} *EA* :
 $\{question, \{question\}_{SSK_{committee}}, time_{x1}\}_{PK_{MIX}}$

Candidate Registration

- 3 - *EA* checks C 's eligibility, and calculates $\tilde{p} = (PK_C)^s$
- 4 - *EA* \rightarrow *NET* : $\{\tilde{p}, g_C\}$
- 5- *NET* calculates $p' = \tilde{p}^r$, and $r = g_C^r$, and stores $time_{nt}$
- 6 - *NET* \rightarrow C : $\{p', r\}$
- 7 - C calculates $p = r^{SK_C}$
- 8 - *EA* \longleftrightarrow C : $ZKP_{eq}((p, p'), (g, h))$ // C 's pseudonym: (r, p, p')

Huszti's Protocol

Examiner Registration

- 9 - EA checks E 's eligibility, and calculates $\tilde{q} = (PK_E)^s$
- 10 - EA $\rightarrow E : \{\tilde{q}, g_E\}$
- 11 - E calculates $q' = \tilde{q}^\alpha$, $t = g_E^\alpha$, and $q = t^{SK_E}$
- 12 - EA $\longleftrightarrow E : ZKP_{eq}((q, q'), (g, h))$ 13 - $E \rightarrow EA : \{t, q, q', h\}$
- 14 - EA checks $q^s = q'$
- 15 - $E \longleftrightarrow EA : ZKP_{sec}(SK_E)$
- 16 - EA stores $\{ID_E, PK_E\}_{PK_{MIX}}, h$

Examination

- 17 - $C \rightarrow EA : \{r, p, p', h\}$
- 18 - EA checks $p^s = p'$
- 19 - $C \longleftrightarrow EA : ZKP_{sec}(SK_C)$
- 20 - EA $\rightarrow C : \{question, \{question\}_{SSK_{committee}}, time_{x1}\}_{PK_{MIX}}$
- 21 - $C \rightarrow EA : \{r, p, \{answer\}_{PK_{MIX}}, time_{x2}\}$
- 22 - EA $\rightarrow C : Hash(r, p, p', h, trans_C, question, time_{x1}, time_{x2}, \{answer\}_{PK_{MIX}})$

Huszti's Protocol

Marking

23 - $EA \rightarrow E : \{answer\}_{PK_{MIX}}$ // Note that EA stored $\{ID_E, PK_E\}_{PK_{MIX}}, h)$

24 - $E \rightarrow EA :$

$\{mark, Hash(mark, answer), [Hash(mark, answer)]^{SK_E}, verzkp, t, q\}$

25 - $E \longleftrightarrow EA :$

$ZKP_{eq}(Hash(mark, answer), [Hash(mark, answer)]^{SK_E}, (t, q))$

Notification

26 - $EA \rightarrow NET : \{p'\}$ // Note that $r = g_C^\Gamma$, $p = PK_C^\Gamma$, $p' = g_C^{\Gamma s}$

27 - NET calculates $p' = \tilde{p}^\Gamma$

28 - $NET \rightarrow EA : \{p', \tilde{p}\}$

29 - EA publishes $mark, Hash(mark, answer), [Hash(mark, answer)]^{SK_E}, verzkp$